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% Simulating the 1-D Diffusion equation (Fourier's equation) by the
...Finite Difference Method(a time march)
% Numerical scheme used is a first order upwind in time and a second order
...central difference in space (both Implicit and Explicit)

%%
%Specifying Parameters
nx=100;           %Number of steps in space(x)
nt=300;          %Number of time steps
dt=0.1;          %Width of each time step
dx=2/(nx-1);     %Width of space step
x=0:dx:2;        %Range of x (0,2) and specifying the grid points
u=zeros(nx,1);   %Preallocating u
un=zeros(nx,1);  %Preallocating un
vis=0.01;        %Diffusion coefficient/viscosity
beta=vis*dt/(dx*dx); %Stability criterion (0<=beta<=0.5, for explicit)
UL=0;            %Left Dirichlet B.C
UR=0;            %Right Dirichlet B.C
UnL=0;           %Left Neumann B.C (du/dn=UnL)
UnR=0;           %Right Neumann B.C (du/dn=UnR)

Cond=1; %1 if dirichlet, 0 if Neumann

%%
%Initial Conditions: A square wave
for i=1:nx
    if ((0.75<=x(i))&&(x(i)<=1.25))
        u(i)=2;
    else
        u(i)=1;
    end
end

%Source
source=zeros(nx-2,nt+1);

for jt=1:nt+1
for jx=1:nx-2

source(jx,jt)=0.05*exp(-((x(jx+1)-1.3)/0.5).^2);
end
end

%%
%B.C vector
bc=zeros(nx-2,1);
if (Cond>0)
bc(1)=vis*dt*UL/dx^2; bc(nx-2)=vis*dt*UR/dx^2; %Dirichlet B.Cs
end
if (Cond==0)
bc(1)=-UnL*vis*dt/dx; bc(nx-2)=UnR*vis*dt/dx; %Neumann B.Cs
end
%Calculating the coefficient matrix for the implicit scheme
E=sparse(2:nx-2,1:nx-3,1,nx-2,nx-2);
if (Cond>0)
A=E+E'-2*speye(nx-2); %Dirichlet B.Cs
end

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if (Cond==0)
A(1,1)=-1; A(nx-2,nx-2)=-1; %Neumann B.Cs
end
D=speye(nx-2)-(vis*dt/dx^2)*A;

%%
%Calculating the velocity profile for each time step
i=2:nx-1;
for it=0:nt
pause(0.1)
un=u;
h=plot(x,u,'k','linewidth',2); %plotting the velocity profile
axis([0 2 0 3])
title(['1-D Diffusion with \nu = ',num2str(vis),' and \beta = ',num2str(beta)];
['time(\itt) = ',num2str(dt*it)])
xlabel('Spatial co-ordinate (x) \rightarrow')
ylabel('Transport property profile (u) \rightarrow')
drawnow;
refreshdata(h)
%Uncomment as necessary
%-----
%Implicit solution

U=un;U(1)=[];U(end)=[];
U=U+bc+dt*source(:,jt);
U=D\U;

if (Cond>0)
u=[UL;U;UR];
end

                if (Cond==0)
u=[U(1)-UnL*dx;U;U(end)+UnR*dx]; %Neumann
end
%}
%-----
%Explicit method with F.D in time and C.D in space
%{
u(i)=un(i)+(vis*dt*(un(i+1)-2*un(i)+un(i-1)))/(dx*dx));
%}
end

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